



**Oscillatory Brain Waves:  
Mechanisms, Functions, and Clinical Perspectives**

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# EEG brain networks for epilepsy applications [Graph Signal Processing]

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# EEG and epilepsy

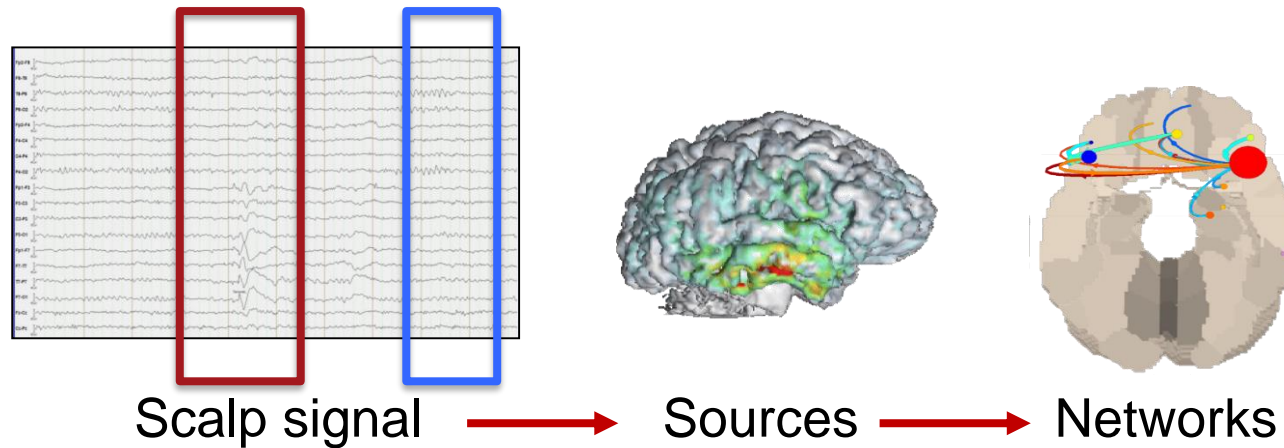
## EEG:

- Directly measures neuronal activity
- Cost-effective, non-invasive, portable
- Low/high-density coverage
- Electrical source imaging (ESI)

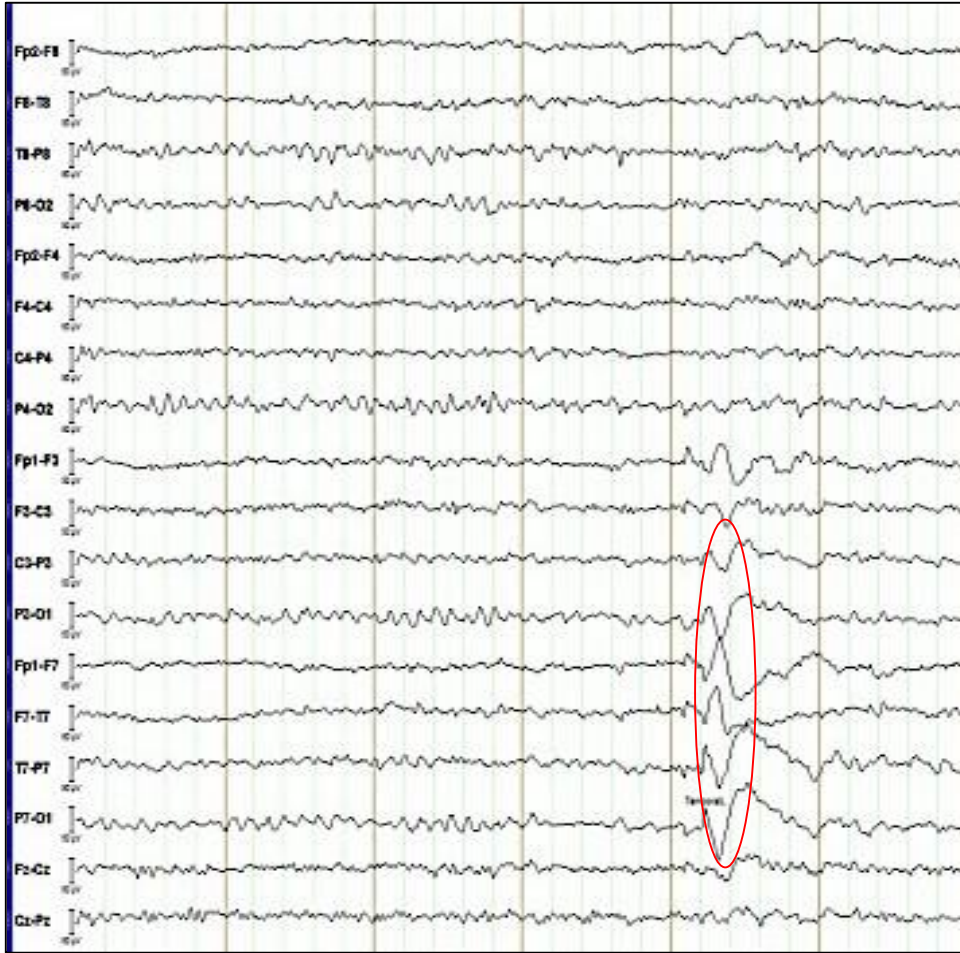


## Epilepsy:

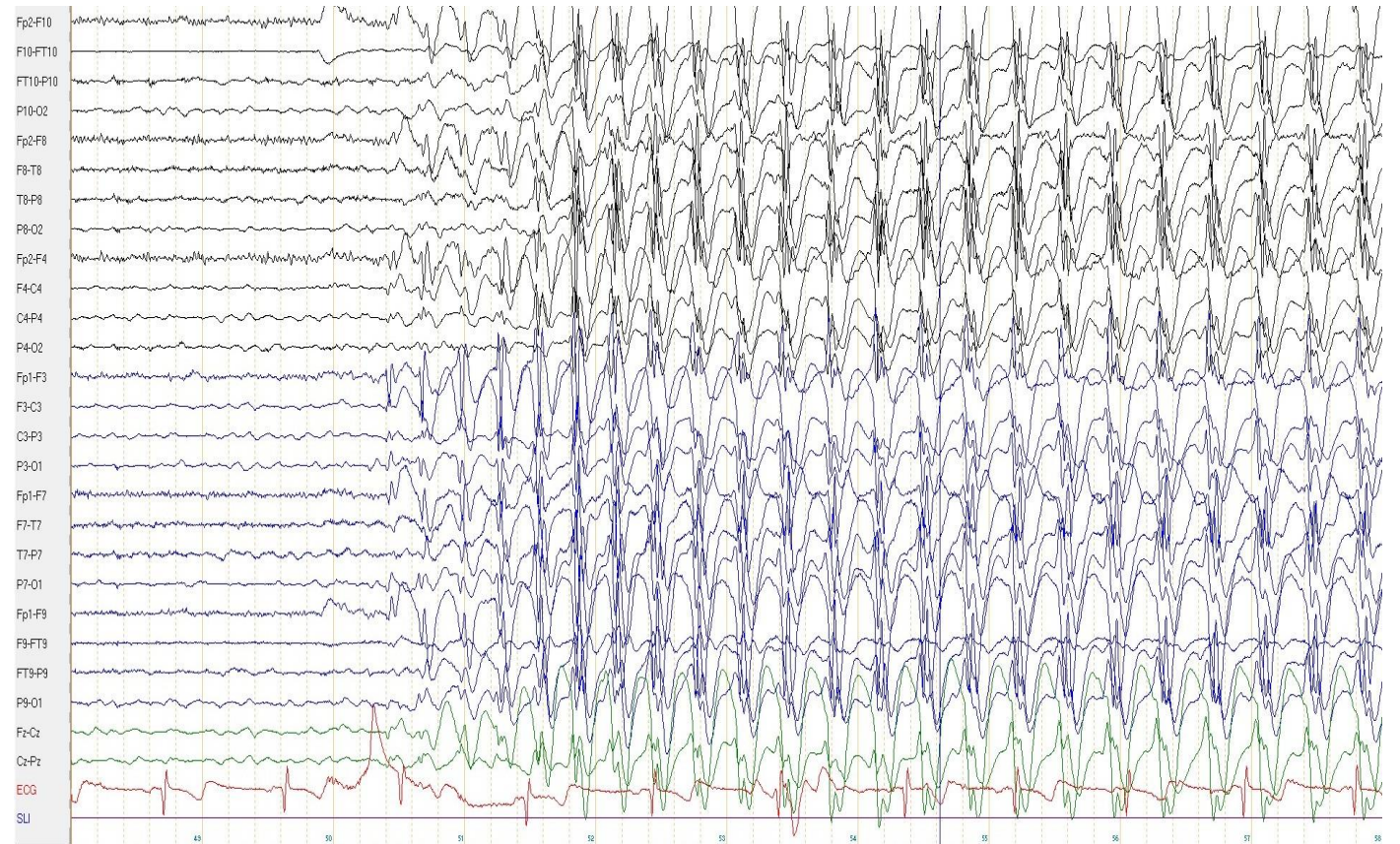
- Neurological disorder characterized by recurrent unprovoked seizures
- Interictal activity: **spikes** (asymptomatic)
- ESI for spike **localisation** (irritative network), presurgical routine
- Brain network disorder
- EEG → **Biomarkers** for **diagnosis** and **prognosis**



# Clinical recordings - examples



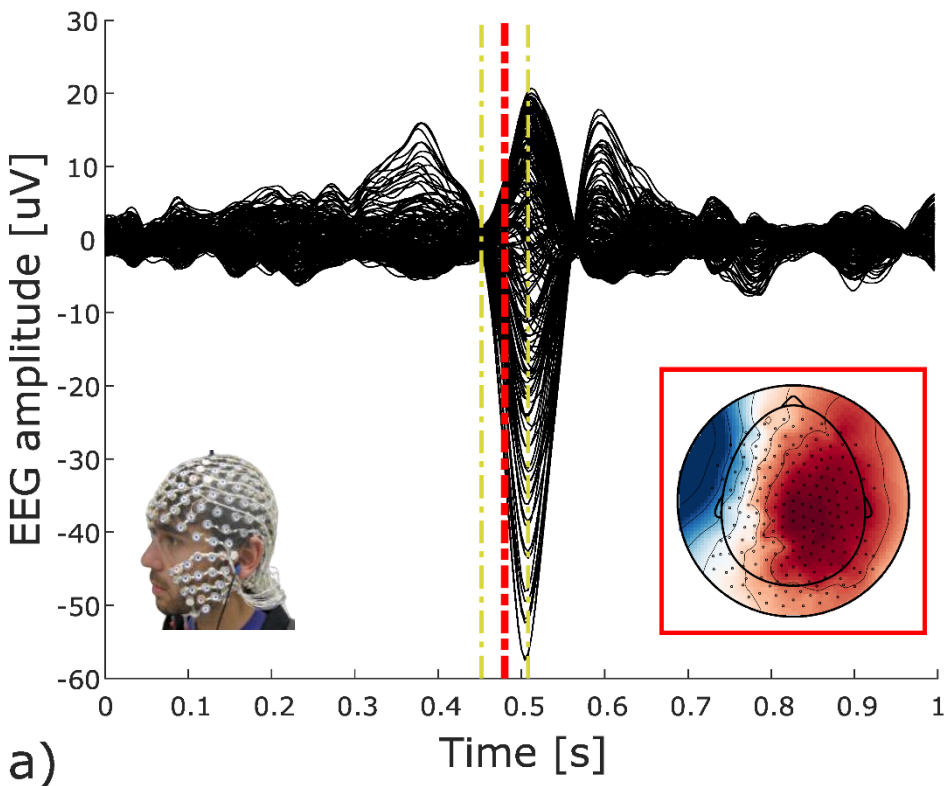
Focal interictal spike



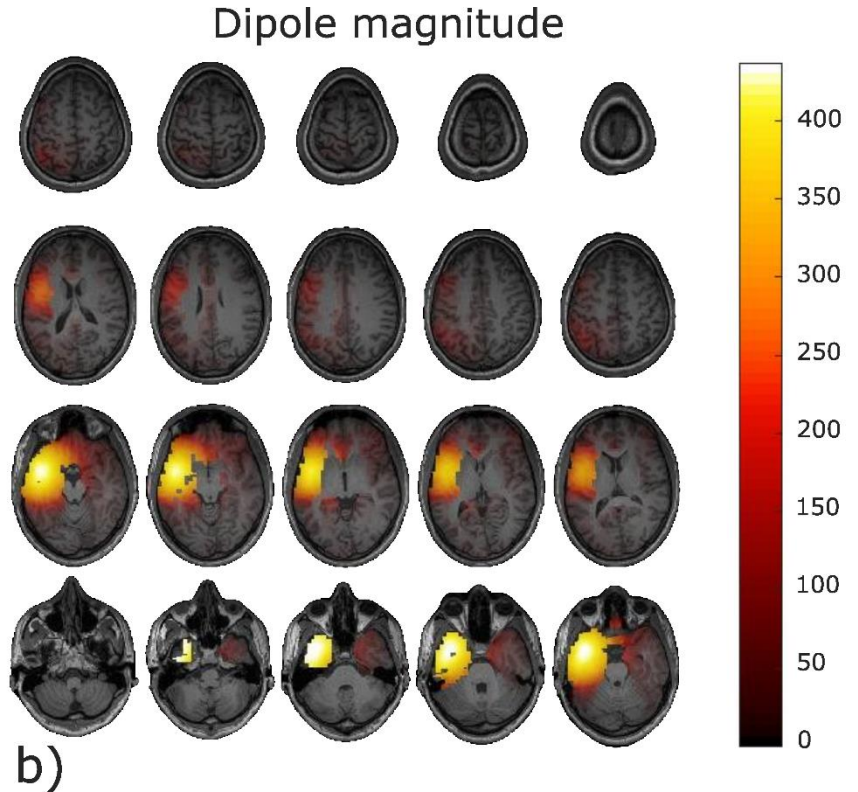
Generalised seizure



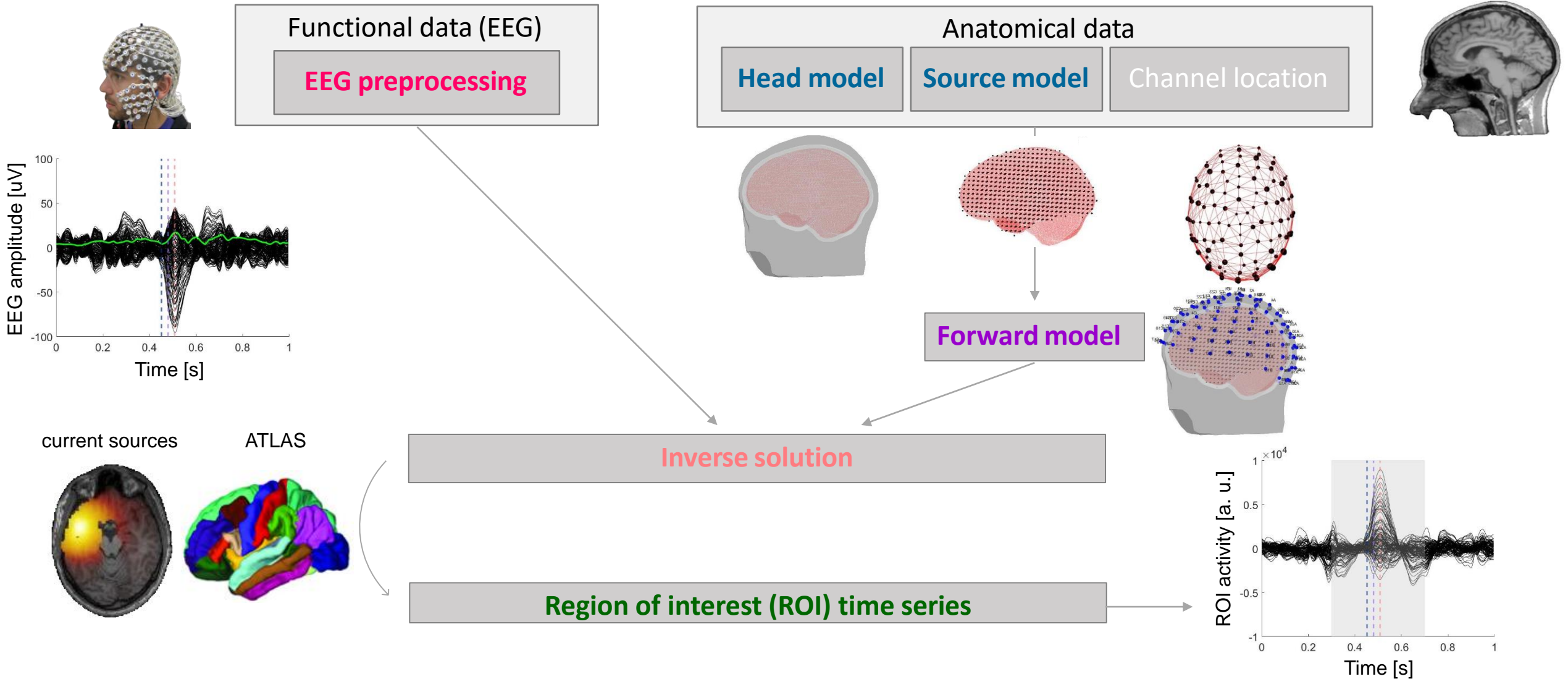
# ESI: get signals *in* the brain from EEG



Electrical Source Imaging (ESI)



# Electrical Source Imaging



# Electrical Source Imaging

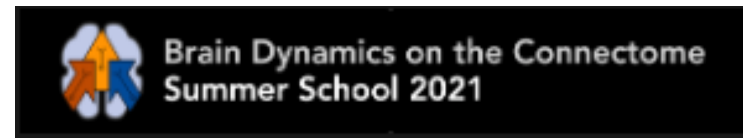


## Tutorial: **from scalp to sources**

Presentation + hands on exercises

Open Matlab code (Fieldtrip)

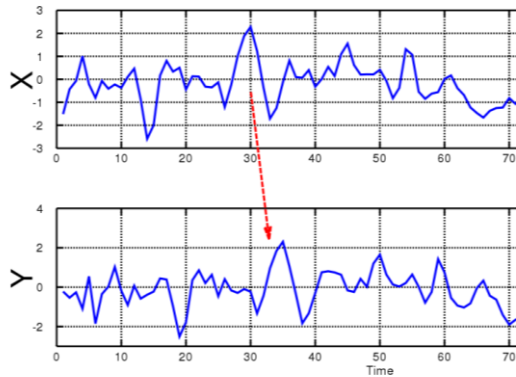
Authors: Isotta Rigoni & Nicolas Roehri



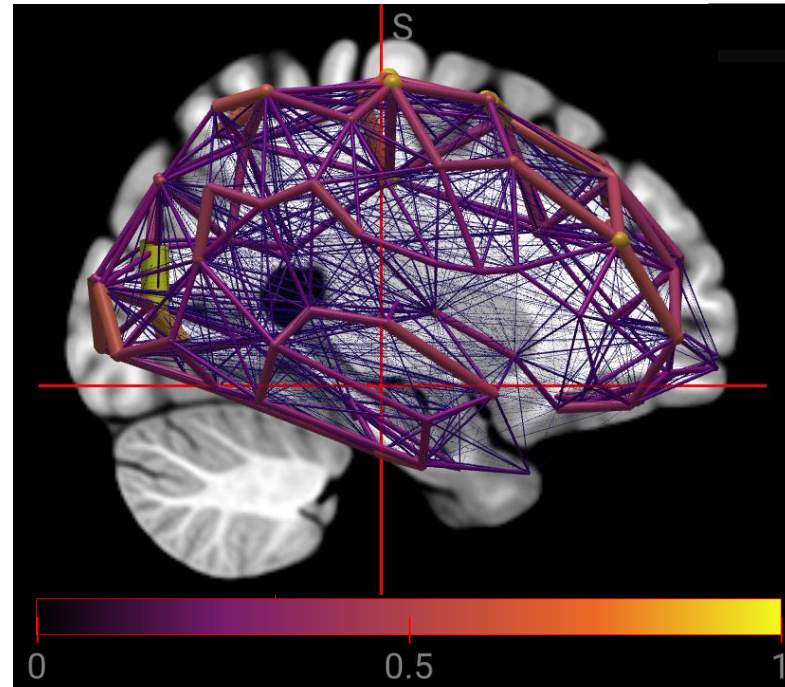
# Connectivity in the brain

## Connectivity metrics

- Amplitude-based
- Phase-based
- Granger causality

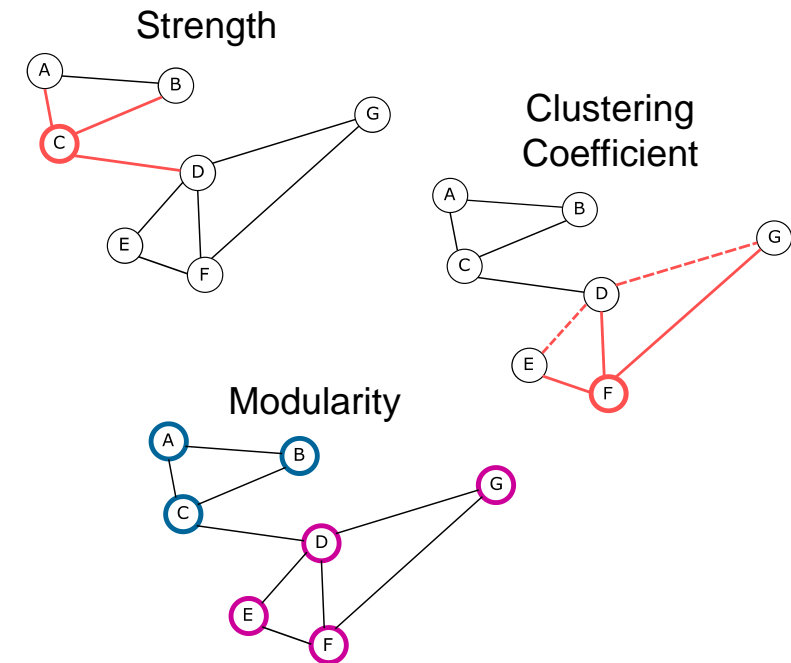


## Brain network



## Graph analyses

- Integration (GE)
- Segregation (CC)
- Whole-brain and nodal measures



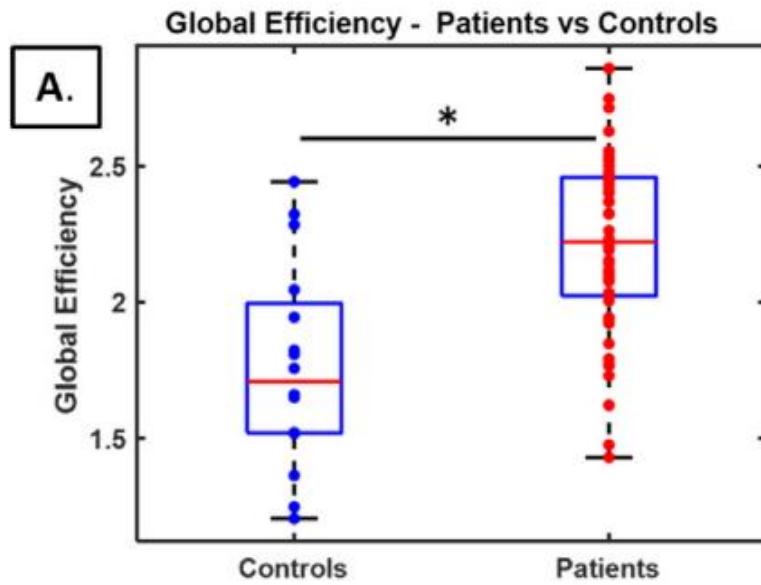
# Is EEG connectivity useful for epilepsy?



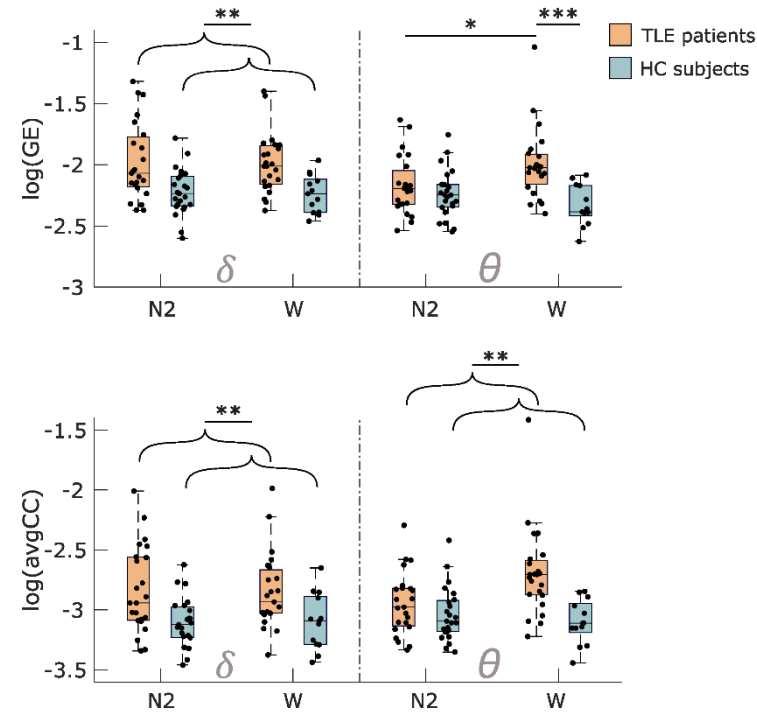
# Epilepsy – diagnostic value of connectivity

Investigate connectivity of spike-free interictal activity with HD-EEG in TLE patients

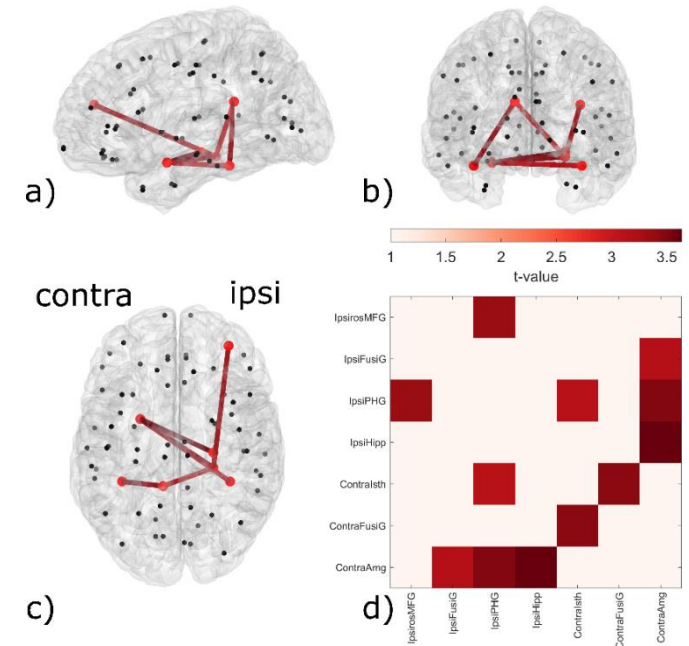
→ global efficiency of the network is higher in patients than in controls at the low frequency bands (delta and theta); easier detection during wake



*Carboni et al. 2020*



*Rigoni et al. 2024*



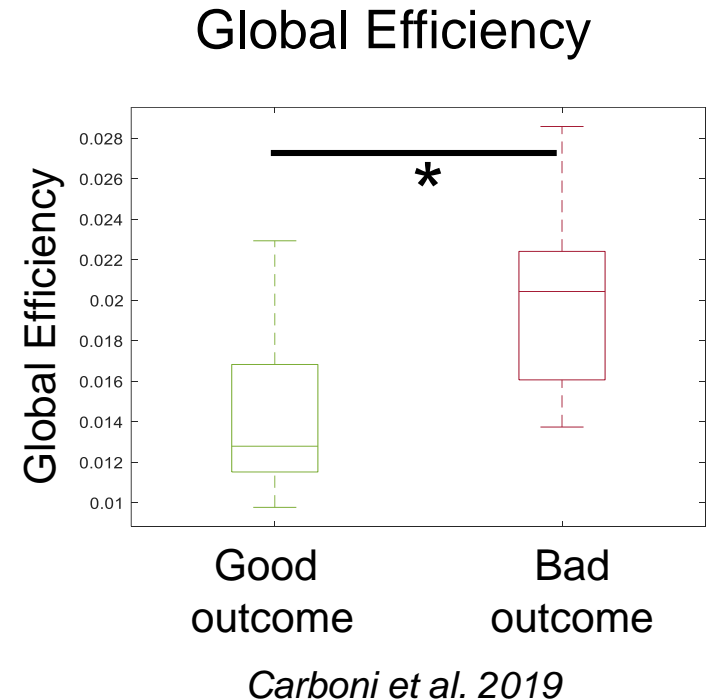
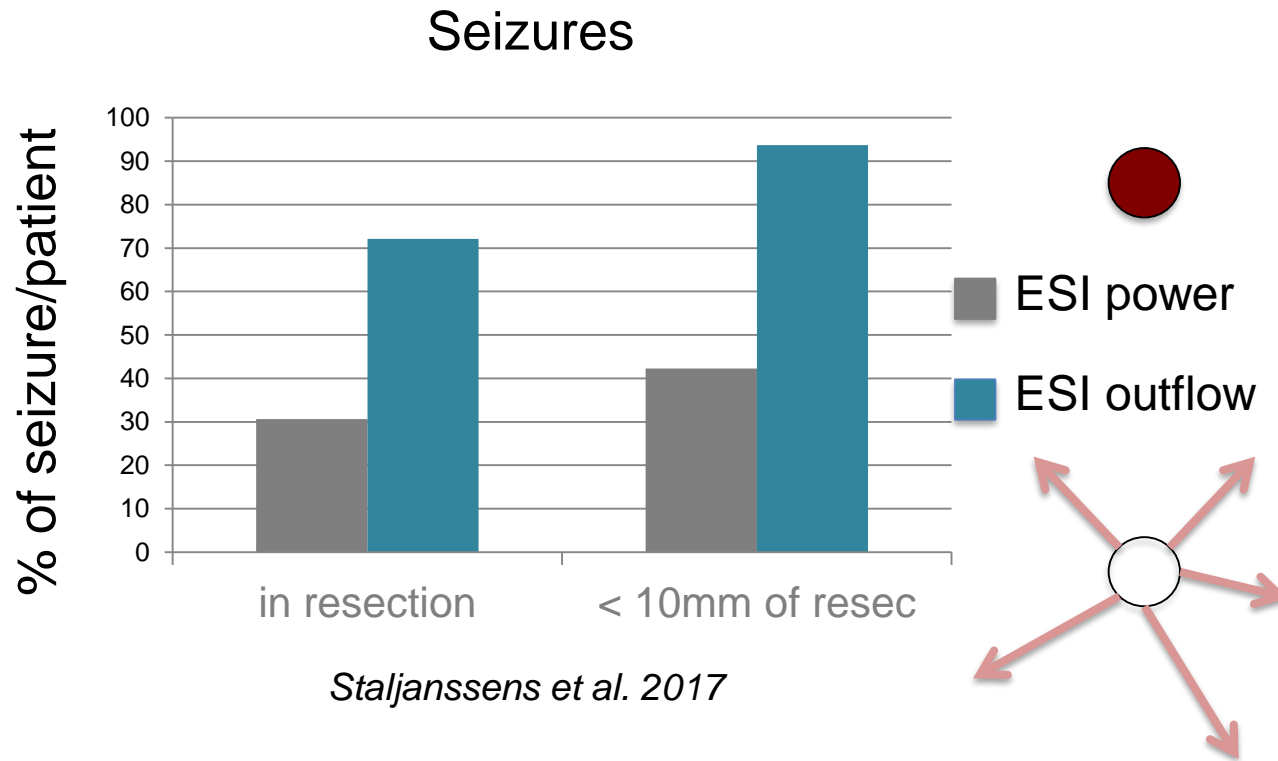
# Epilepsy – prognostic value of connectivity

Investigate connectivity added value for localization of seizure onset zone (seizure-free patients)

→ Summed outflow metric provided a significant added value to ESI alone

Investigate connectivity of spikes for surgical outcome prediction

→ Significant difference in network propagation between good-outcome vs bad-outcome

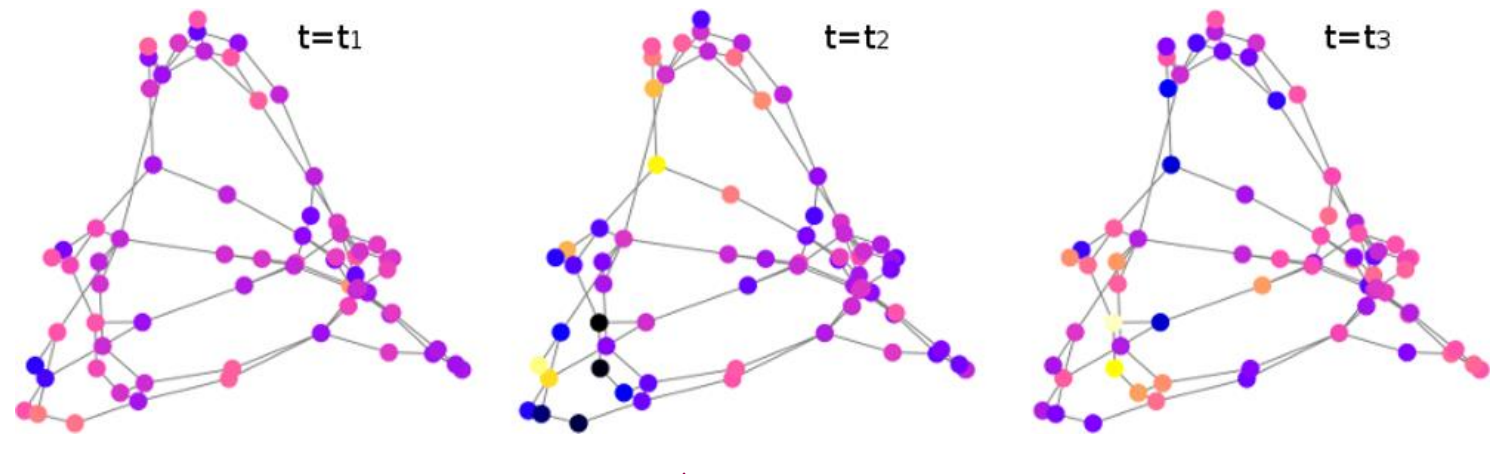
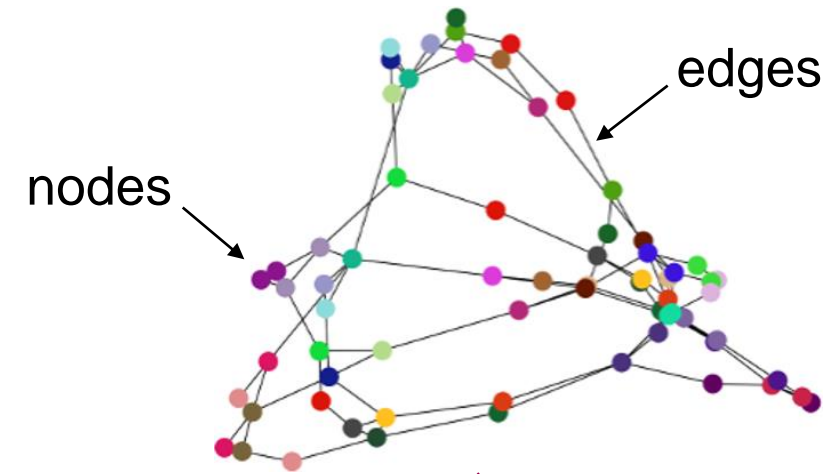


# Graph signal processing

# Graph vs graph signal

## Graph

## Graph signal



↑  
does NOT change  
over time

↑  
the activity of each node  
changes over time

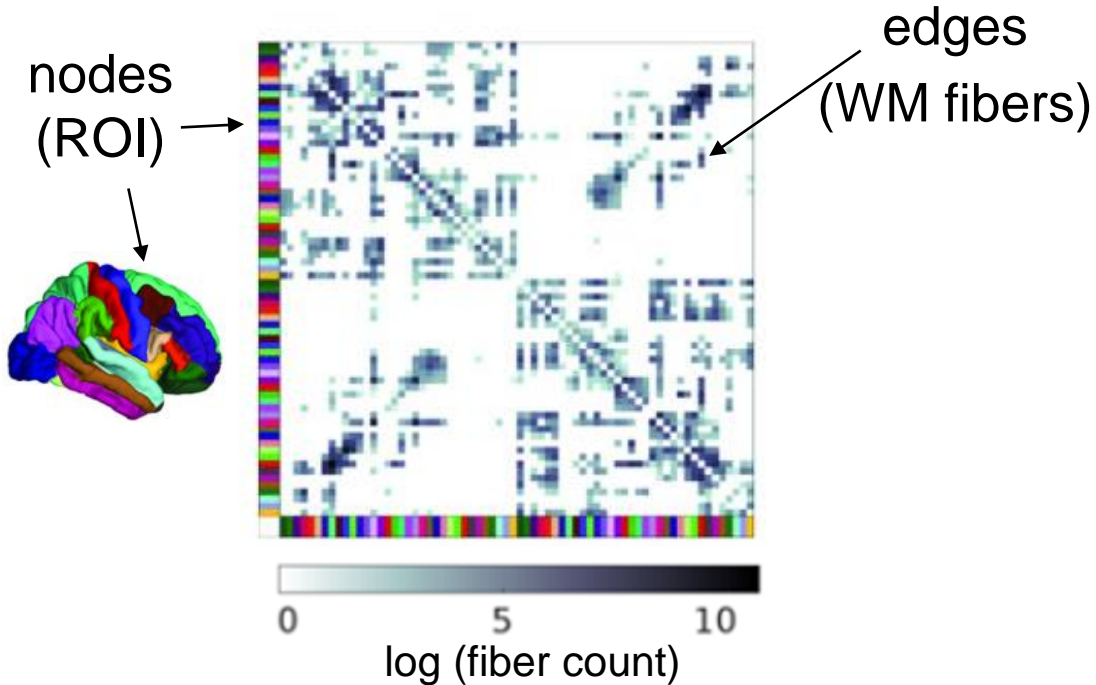
*Figures adapted from Glomb 2020*



# Graph vs graph signal – brain data

Graph:

**Structural connectome**



Graph signal:

**Functional brain signal**

- BOLD
- Reconstructed EEG

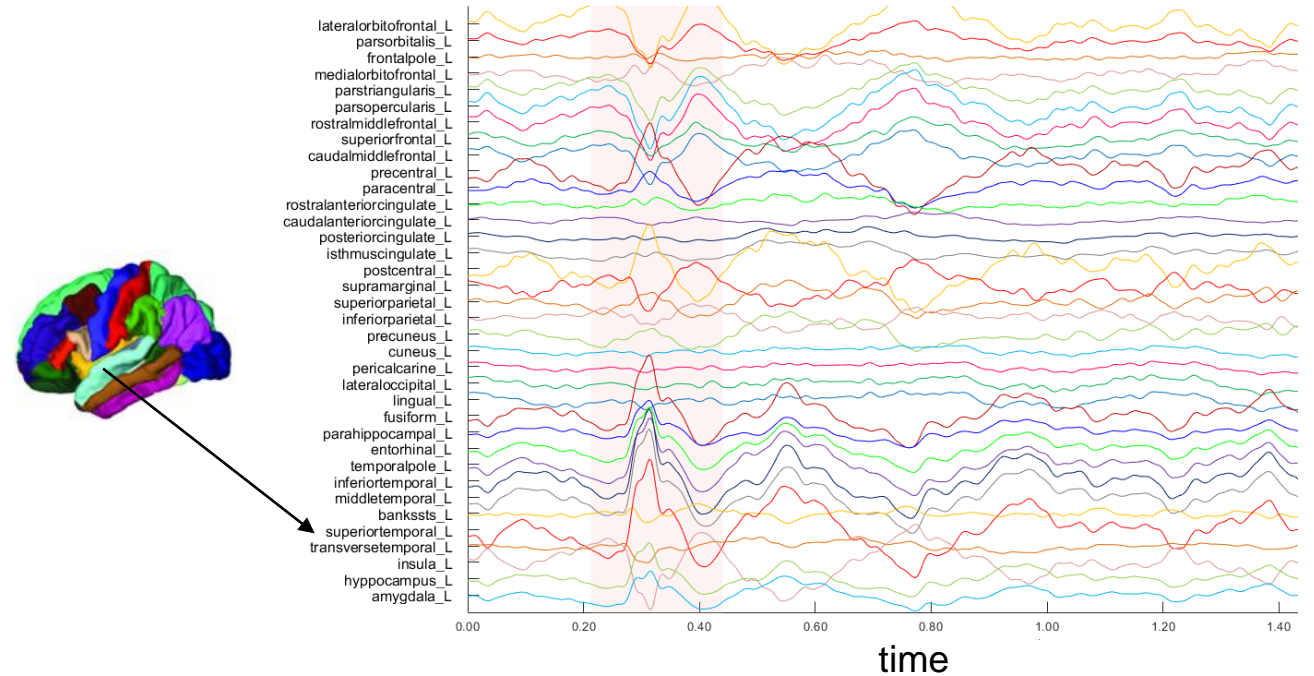
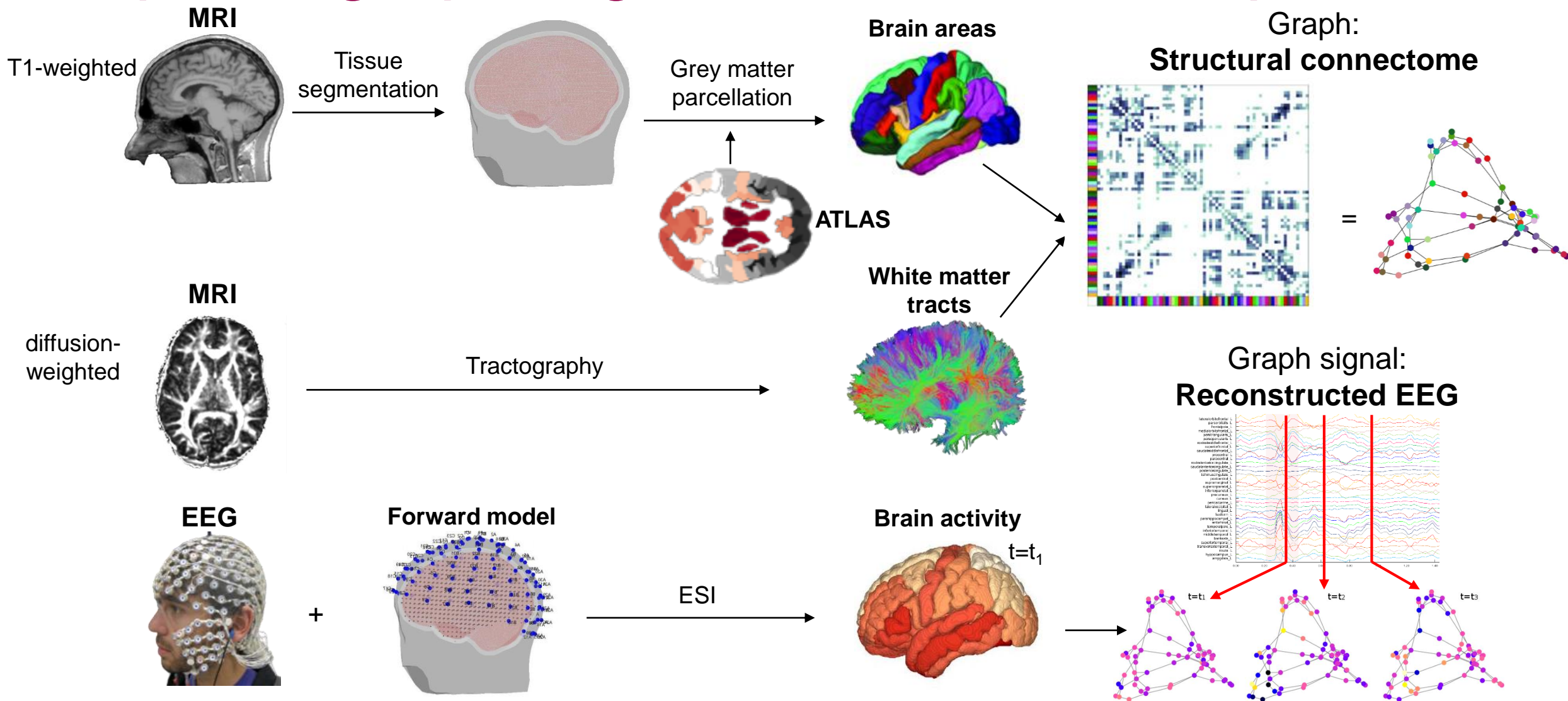


Figure adapted from Glomb 2020

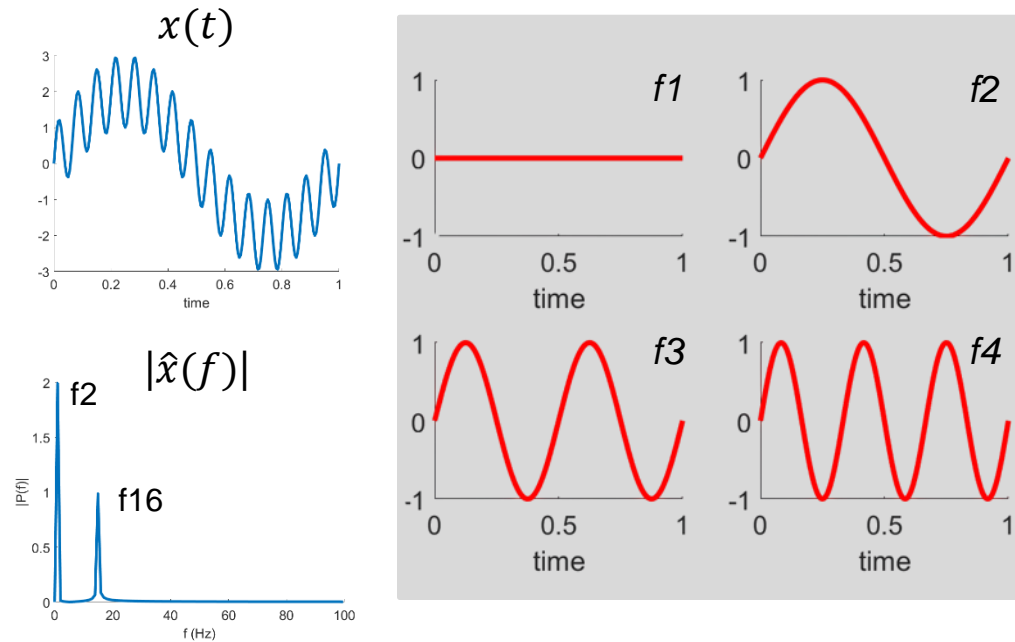
# Graph vs graph signal – brain data in practice



# Fourier transform

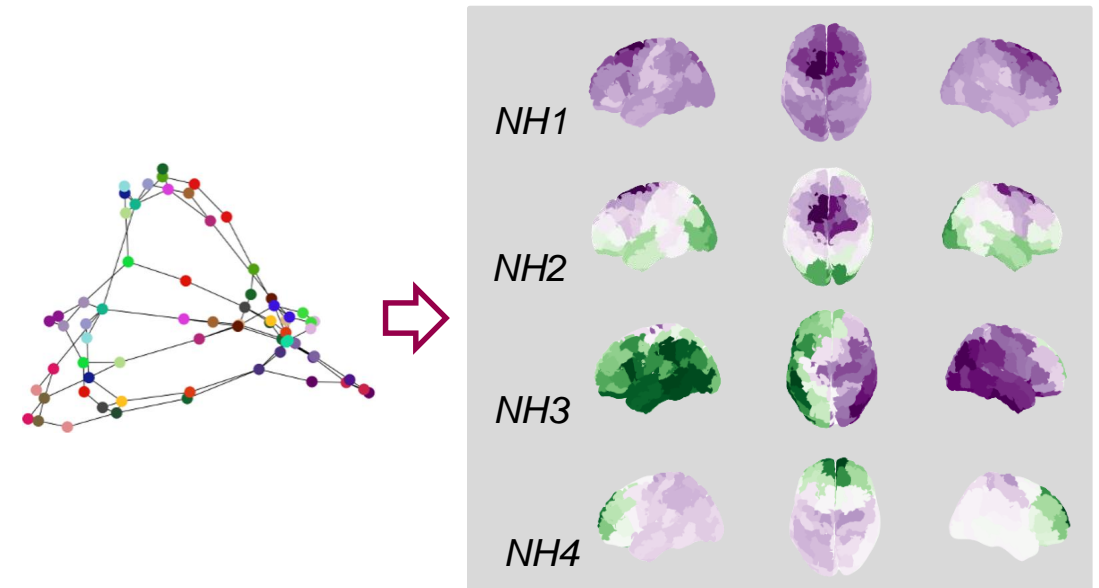
## In time domain

- One dimensional signal defined over time
- The time graph can be decomposed into sine and cosine waves (Fourier modes)
- The signal can be reconstructed as a linear combination of these modes



## In graph domain:

- Graph signal (reconstructed EEG) is defined over a graph
- The (structural) graph can be decomposed into Fourier modes -*network harmonics (NH)*-
- The graph signal can be reconstructed as a linear combination of these harmonics



# Fourier transform – time domain

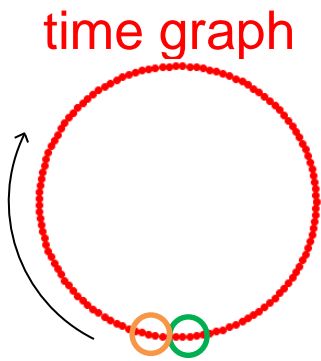
Where do these Fourier modes ( $f_1, f_2$  etc.) come from?

→ They are the eigenvectors of the graph Laplacian of the [time graph](#)

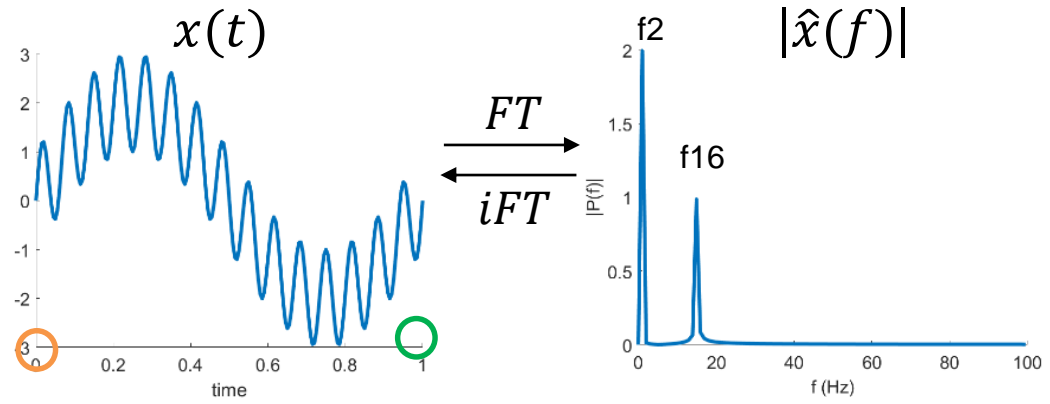
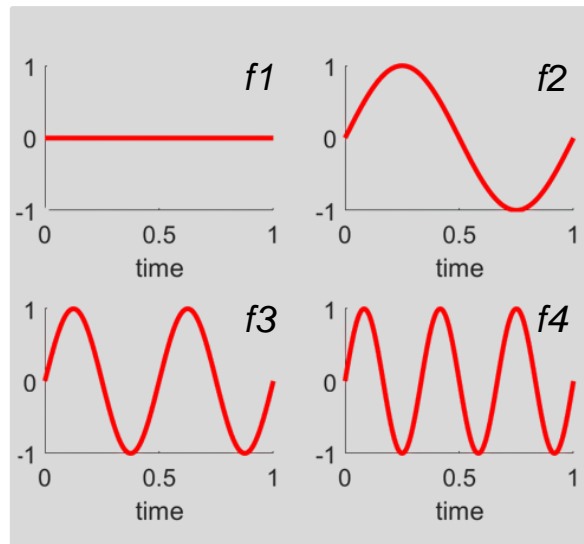
$$\hat{x}(f) = \int_{-\infty}^{\infty} x(t) * e^{-2\pi i f t} dt$$
$$x(t) = \int_{-\infty}^{\infty} \hat{x}(f) * e^{2\pi i f t} df$$

What is the **time graph**?

- Stationary time is modelled as a 1-d ring graph
- First and last point of signal are connected



graph Laplacian



We can write the time-series as a linear weighted combination of these Fourier modes and understand the frequency content of the signal

→ These are *time frequencies*

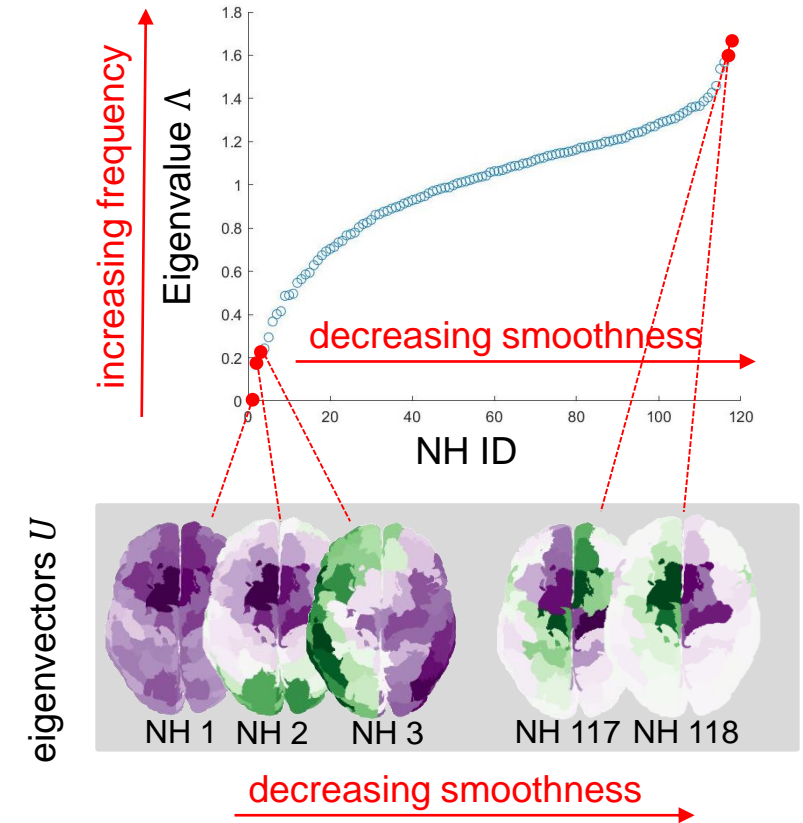
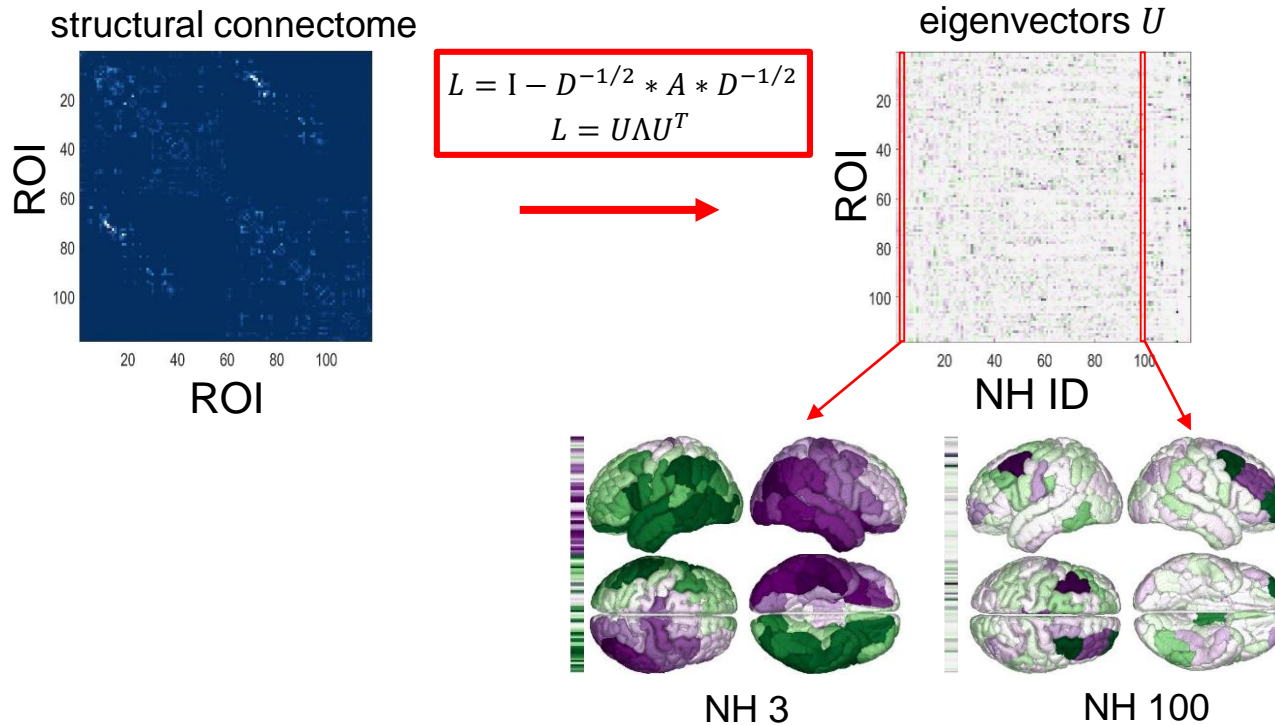


And in the graph domain?

# Fourier transform – graph domain

## Graph Fourier transform (GFT):

- The EEG-signal lives on the structural connectome
- Calculate the graph Laplacian of the structural connectome
- Eigendecompose the graph Laplacian and extract the Fourier modes or “*network harmonics*” (NH)



→ These are *spatial frequencies*

# Fourier transform – graph domain

Graph Fourier transform the reconstructed EEG:

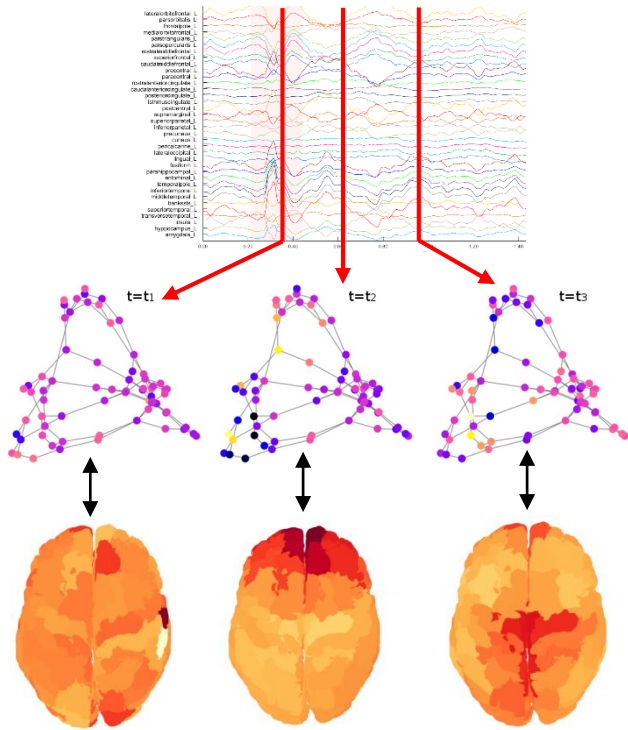
- Multiply the network harmonics by the signal in the ROI space  $x_R(t)$
- $x_R(t)$  can be recovered by the inverse operation (inverse GFT)

connectome spectrum of the signal  $x_R(t)$

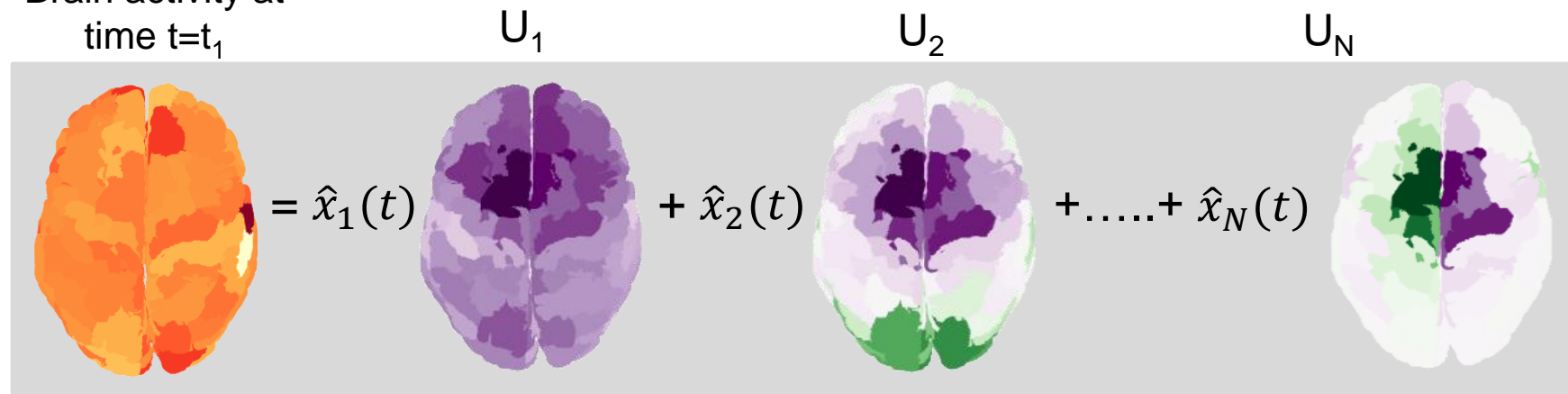
$$\hat{x}_\lambda(t) = U^T * x_R(t) \quad \leftarrow \text{GFT}$$

$$x_R(t) = U * \hat{x}_\lambda(t) \quad \leftarrow \text{Inverse GFT}$$

Graph signal:  
Reconstructed EEG



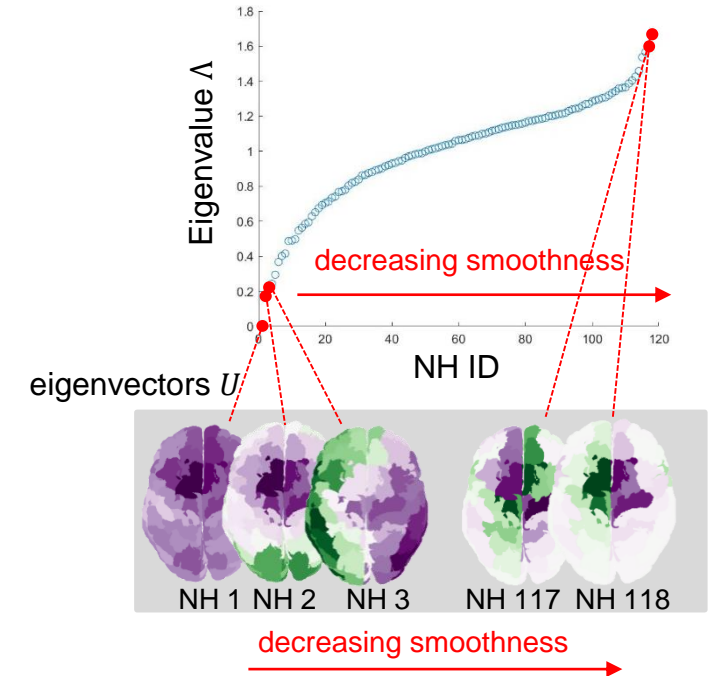
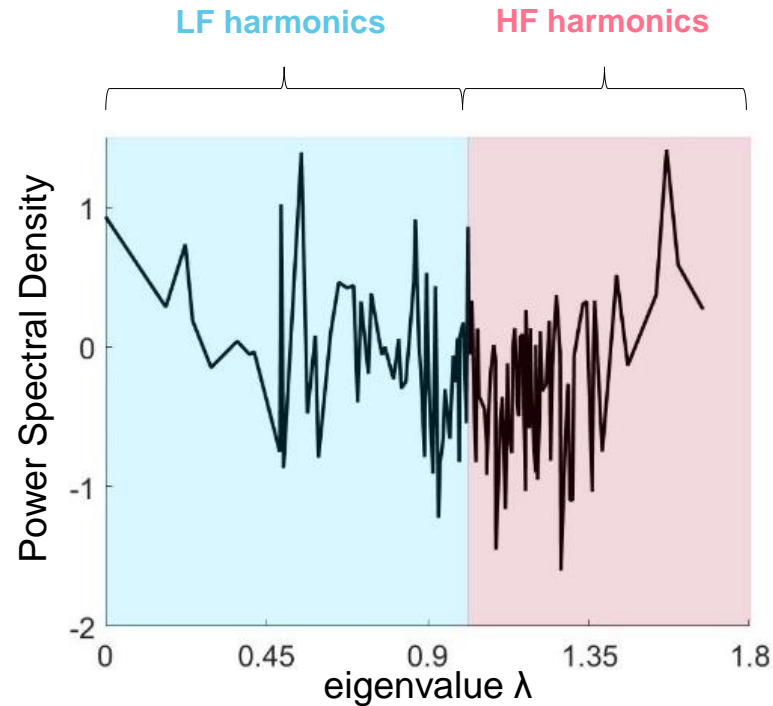
Brain activity at time  $t=t_1$



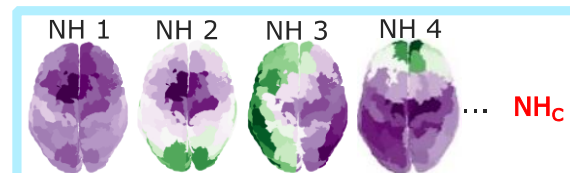
Functional activity decomposition

# Graph filtering – spectrum dichotomization

- In classic EEG analyses there are frequency bands of interest
- In the graph domain we have *spatial frequencies* (not time frequencies)
- We split the connectome spectrum in two parts of equal cumulative power:
  - **low-frequency harmonics**
  - **high-frequency harmonics**

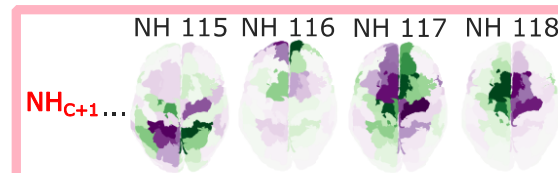


smooth spatial maps



integrative patterns

coarse spatial maps



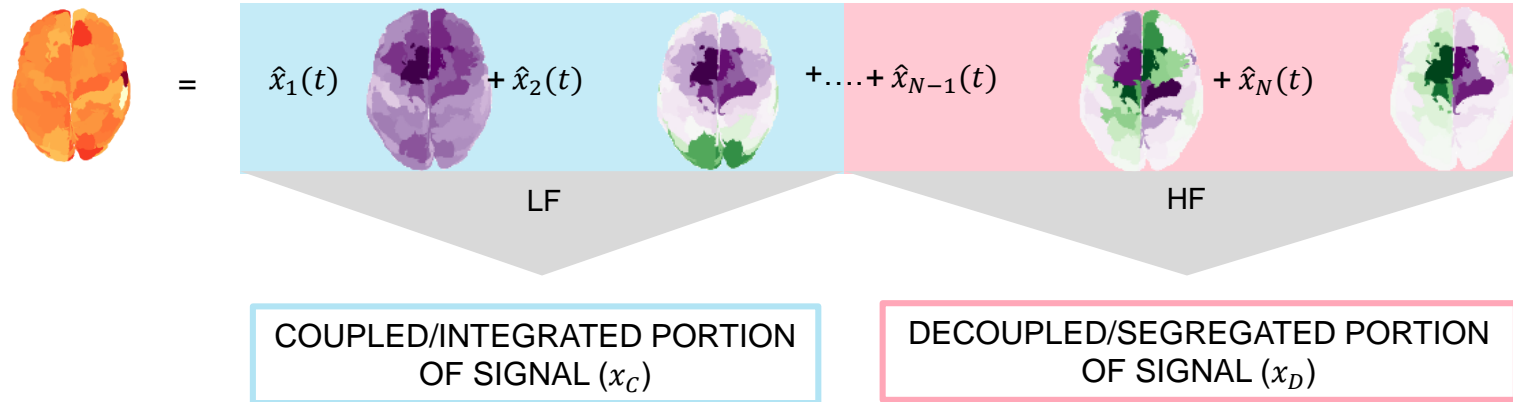
segregative patterns



# Graph filtering and SDI

- Filter EEG reconstructed signal using one subset of frequencies:
  - **low-frequency harmonics:**  $x_R(t) = U_{LF} * \hat{x}_\lambda(t)$
  - **high-frequency harmonics:**  $x_R(t) = U_{HF} * \hat{x}_\lambda(t)$
- Get structural decoupling index (SDI) as ratio of the two signals

Brain activity at time  $t$



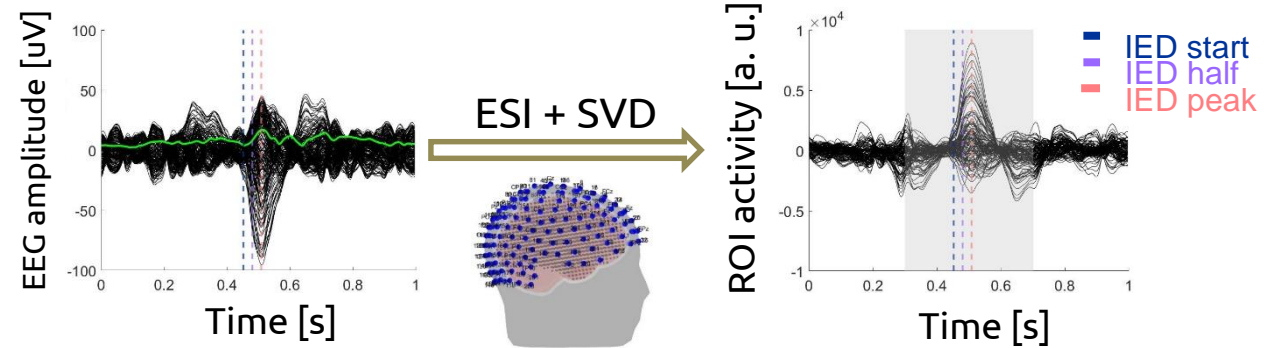
$$\text{STRUCTURAL-DECOUPLING INDEX} = \frac{\text{DECOUPLING}}{\text{COUPLING}}$$

# Can GSP predict the surgical outcome?

# Study 1: GSP on interictal spikes

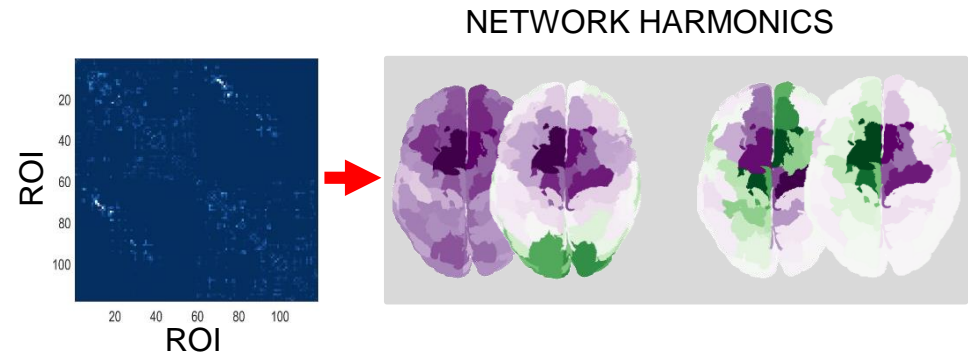
## The functional data

- 9 RTLE and 8 LTLE patients
- HD EEG and structural MRI
- IEDs marked and extracted
- Activity of each ROI was reconstructed via ESI



## The structural data

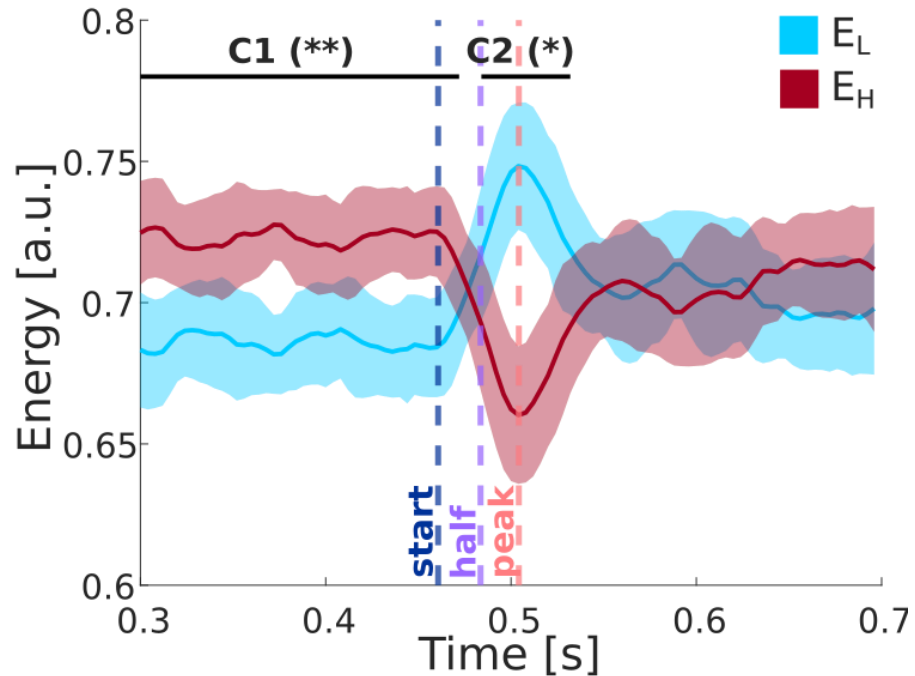
- Consensus structural connectome (SC) from 70 healthy subjects
- Extract network harmonics (NH) as eigenvectors of the SC Laplacian and divide them in low/high frequency harmonics



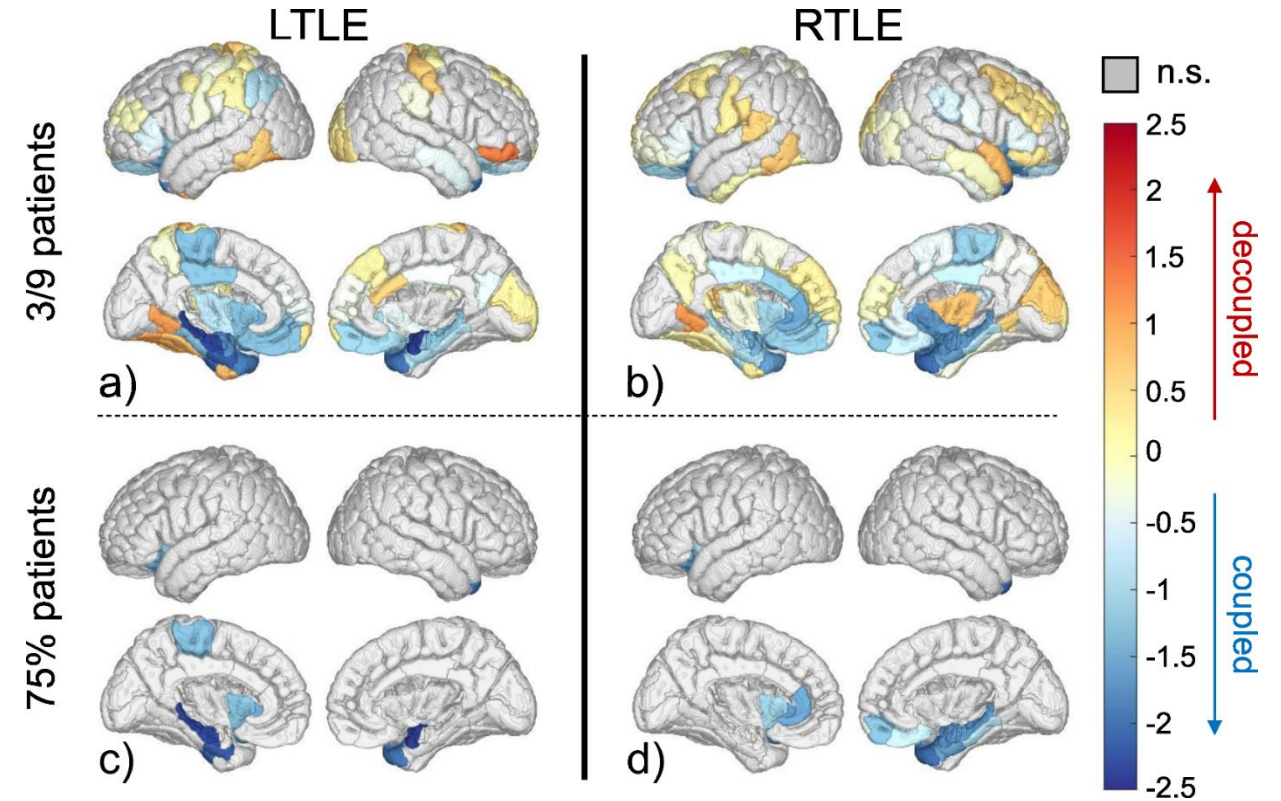
Rigoni et al. 2023

# Study 1: GSP on interictal spikes

- **C1**: most energy of the EEG signal is in the HF harmonics (**coarse spatial maps**) → **segregation**
- **C2**: predominance of LF harmonics (**smooth spatial maps**) → **integration**



- Activity in ipsilateral mesial temporal ROI is more coupled to the structure in 75% of patients than the best performing surrogate along the whole IED duration



Rigoni et al. 2023

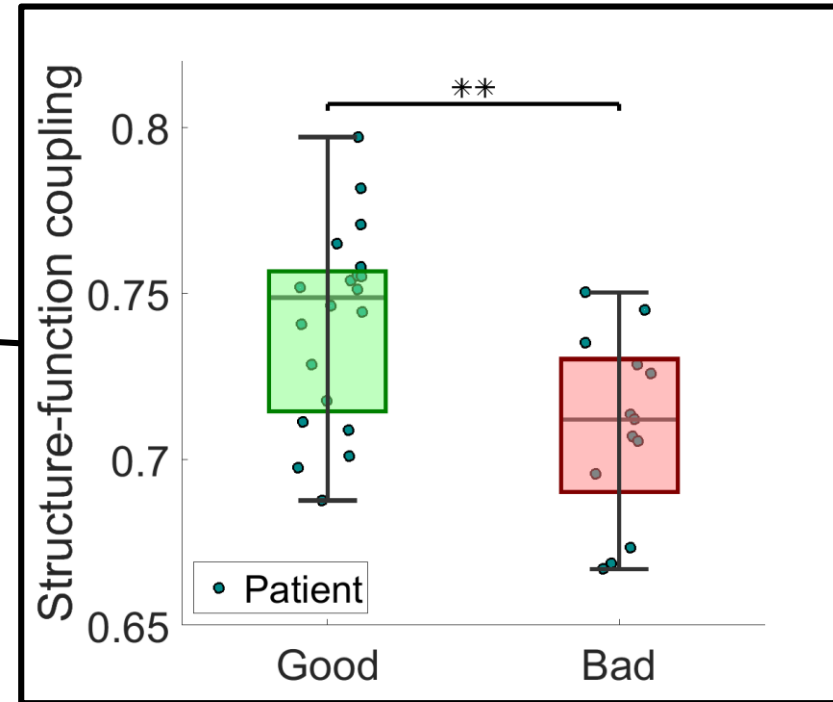
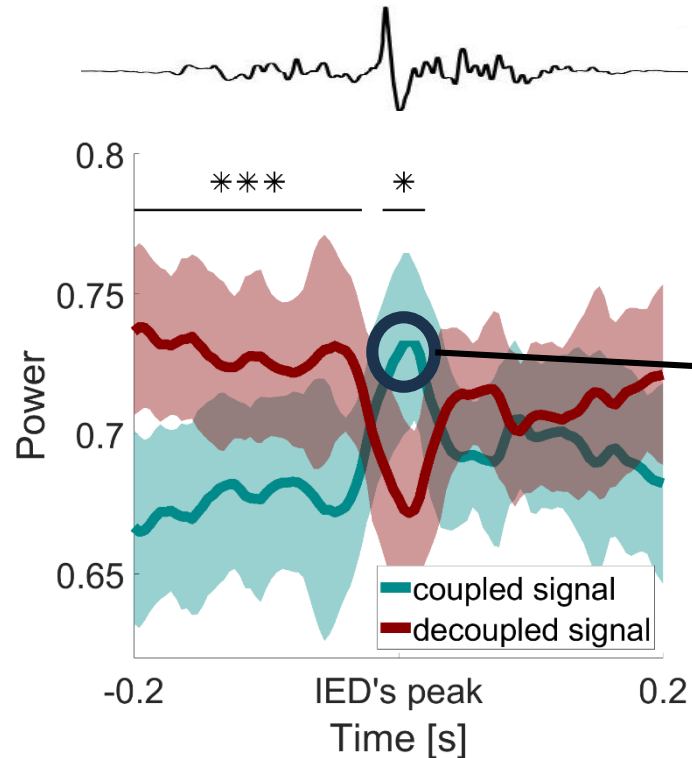


# Study 2: GSP on interictal spikes

- 33 patients with temporal lobe epilepsy, operated, with surgical outcome at 1 year
- Replication of previous results on SDI (coupling/decoupling during IED)
- Coupling during the IED could serve as biomarker for surgical outcome

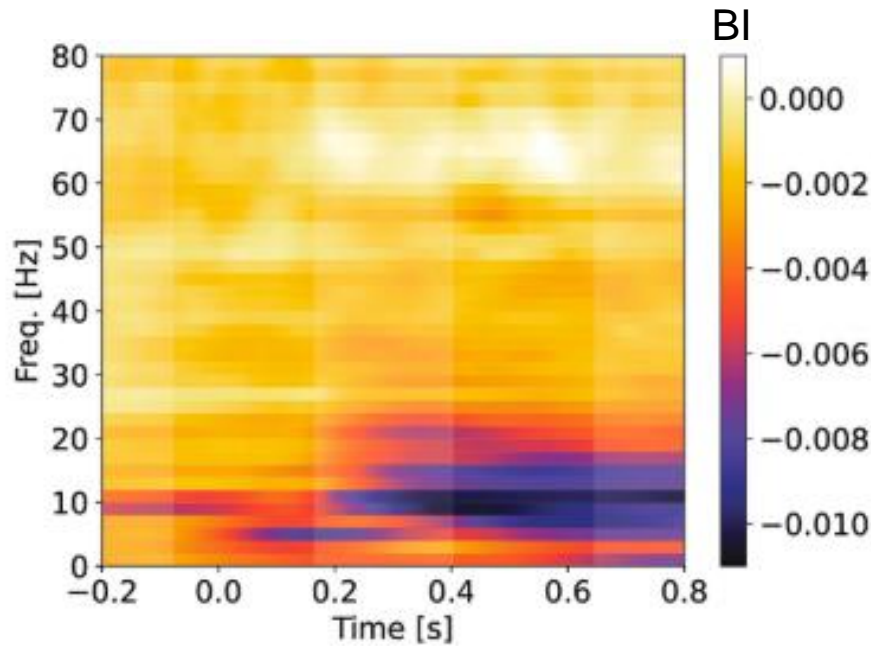
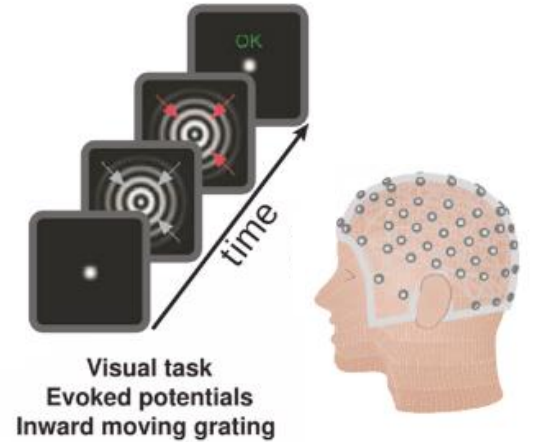
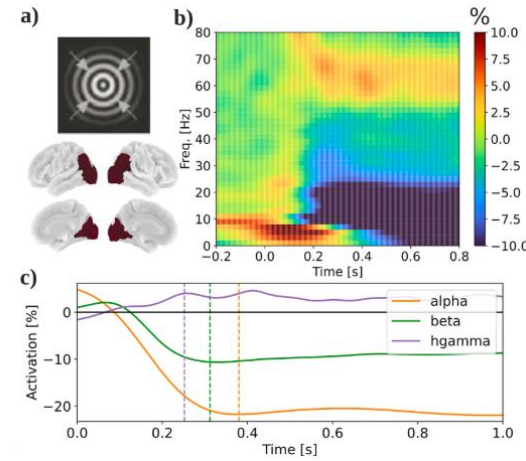


Louise de Wouters  
d'Oplinter



# GSP: spatial- and time- frequencies

- Joint time-vertex connectome spectral analysis  
→ different information processing mechanisms (int/seg) are carried out at different frequency bands
- Broadcasting index (BI) similar to SDI
- **BI > 0 : HF harmonics (segregation)**
- **BI < 0 : LF harmonics (integration)**



↑ segregative patterns  
More localised activity (BI > 0) in high gamma

↓ Dominance of smooth NH in alpha/theta  
integrative patterns

- **localized electrical activity** (i.e., segregation) is observed **at high temporal frequencies** (high and low gamma) over restricted high spatial graph frequencies
- **spatially distributed activity** (i.e. integration) specifically occurs **at low temporal frequencies** (alpha and theta) and low graph spatial frequencies

Rué-Queralt and Mancini et al. 2023

# GSP: references

M. G. Preti and D. Van De Ville, “Decoupling of brain function from structure reveals regional behavioral specialization in humans,” *Nat. Commun.*, vol. 10, no. 1, pp. 1–7, 2019, doi: 10.1038/s41467-019-12765-7.

K. Glomb *et al.*, “Using structural connectivity to augment community structure in EEG functional connectivity,” *Netw. Neurosci.*, vol. 4, no. 3, pp. 761–787, 2020, doi: 10.1162/netn\_a\_00147.

J. Rué-Queralt *et al.*, “The connectome spectrum as a canonical basis for a sparse representation of fast brain activity,” *Neuroimage*, vol. 244, no. September, p. 118611, 2021, doi: 10.1016/j.neuroimage.2021.118611.

I. Rigoni *et al.*, “Structure-function coupling increases during interictal spikes in temporal lobe epilepsy: A graph signal processing study,” *Clin. Neurophysiol.*, vol. 153, pp. 1–10, 2023, doi: 10.1016/j.clinph.2023.05.012.

R. Blanco, M. G. Preti, C. Koba, D. Van De Ville, and A. Crimi, “Comparing structure–function relationships in brain networks using EEG and fNIRS,” *Sci. Rep.*, vol. 14, no. 1, pp. 1–18, 2024, doi: 10.1038/s41598-024-79817-x.

J. Rué-Queralt *et al.*, “The coupling between the spatial and temporal scales of neural processes revealed by a joint time-vertex connectome spectral analysis,” *Neuroimage*, vol. 280, no. March, 2023, doi: 10.1016/j.neuroimage.2023.120337.

Thank you!